Math 30-1: Transformations and Operations PRACTICE EXAM

- 1. If the graph of f(x) undergoes the transformation $y = f(\frac{1}{5}x)$, a point that exists on the graph of the image is:
 - **A.** $\left(\frac{1}{5}, 4\right)$
 - **B.** (2, 1)
 - **C.** (-5, 5)
 - **D.** (6, 0)
- 2. If the graph of f(x) undergoes the transformation x = f(y), an invariant point is:
 - **A.** (7, 1)
 - **B.** (3, -3)
 - **C.** (5, 5)
 - **D.** (3, 1)
- If the graph of f(x) undergoes the transformation y 4 = f(x), then the range of the image is:
 - A. $\{y \mid -6 \le y \le -1, y \in R\}$ B. $\{y \mid 2 \le y \le 7, y \in R\}$ C. [-6, -1] D. (2, 7)
- 4. If the graph of f(x) is horizontally translated 6 units left, then the corresponding transformation equation and mapping are:

A. Transformation Equation: y = f(x - 6); Mapping: $(x, y) \rightarrow (x - 6, y)$ B. Transformation Equation: y = f(x - 6); Mapping: $(x, y) \rightarrow (x + 6, y)$ C. Transformation Equation: y = f(x + 6); Mapping: $(x, y) \rightarrow (x - 6, y)$ D. Transformation Equation: y = f(x + 6); Mapping: $(x, y) \rightarrow (x + 6, y)$









- 5. If f(x) (dashed line ---) is transformed to the image (solid line –), then the corresponding transformation equation and mapping are:
 - A. Transformation Equation: $y = f\left(\frac{1}{2}x\right)$; Mapping: $(x, y) \rightarrow (2x, y)$

B. Transformation Equation: $y = f\left(\frac{1}{2}x\right)$; Mapping: $(x, y) \rightarrow \left(\frac{1}{2}x, y\right)$

C. Transformation Equation: y = f(2x); Mapping: $(x, y) \rightarrow (2x, y)$

D. Transformation Equation: y = f(2x);

Mapping: $(x, y) \rightarrow \left(\frac{1}{2}x, y\right)$



- 6. If the graph of $f(x) = x^2 + 1$ is transformed by g(x) = f(2x), then the function of the image is:
 - A. $g(x) = 4x^2 + 1$ B. $g(x) = 2x^2 + 1$ C. $g(x) = 2x^2 + 2$ D. g(x) = 2x + 1
- 7. If the graph of $f(x) = x^2 4$ is transformed by g(x) = f(x) 4, then the function of the image is:
 - A. $g(x) = x^2 8$ B. $g(x) = x^2$ C. $g(x) = (x - 4)^2 - 4$ D. $g(x) = (x + 4)^2 - 4$
- 8. If the graph of $f(x) = (x + 2)^2$ is horizontally translated so it passes through the point (6, 9), the transformation equation is:
 - **A.** y = f(x 5)
 - **B.** y = f(x 11)
 - **C.** Neither y = f(x 5) nor y = f(x 11).
 - **D.** Both y = f(x 5) and y = f(x 11).



- **9.** Sam sells bread at a farmers' market for \$5.00 per loaf. It costs \$150 to rent a table for one day at the farmers' market, and each loaf of bread costs \$2.00 to produce. The cost (expenses) and revenue functions are:
 - C(n) = 2n + 150 R(n) = 5n

If the cost of renting a table increases by \$50/day, and Sam raises the price of a loaf by 20%, then the new cost and revenue functions are:

- **A.** $C_2(n) = 2n + 200$ and $R_2(n) = n$
- **B.** $C_2(n) = 2.4n + 200$ and $R_2(n) = 6n$
- **C.** $C_2(n) = 2(n 50) + 150$ and $R_2(n) = 5.2n$
- **D.** $C_2(n) = 2n + 200$ and $R_2(n) = 6n$
- A basketball player throws a basketball. The path can be modeled with the function:

$$h(d) = -\frac{1}{9}(d - 4)^2 + 4$$

If the player moves so the equation of the shot is $h(d) = -\frac{1}{9}(d + 1)^2 + 4$, the horizontal distance of the player from the hoop is:

-3

-2

-1

0

1

2

3

- A. 1 metre
- B. 3 metres
- C. 8 metres
- D. 12 metres
- 11. The transformation y = -3f[-4(x 1)] + 2 is best described (sequentially) as:

-5

-4

A. Translations 1 unit left and 2 units up; reflections about both the x- and y-axis; a vertical stretch by a scale factor of 3 and a horizontal stretch by a scale factor of 4.

B. Translations 1 unit right and 2 units up; reflections about both the x- and y-axis; a vertical stretch by a scale factor of 3 and a horizontal stretch by a scale factor of 1/4.

C. Reflections about both the x- and y-axis; a vertical stretch by a scale factor of 1/3 and a horizontal stretch by a scale factor of 4; and translations 1 unit right and 2 units up.

D. A vertical stretch by a scale factor of 3 and a horizontal stretch by a scale factor of 1/4; reflections about both the x- and y-axis; and translations 1 unit right and 2 units up.



 \Box

6

8

9 d





- **12.** If the graph of f(x) undergoes the transformation $y = f[\frac{1}{3}(x 1)] + 1$, the domain and range of the image are:
 - A. D: [-2, 7]; R: [2, 4] B. D: (-2, 7); R: (2, 4) C. D: {x | $2 \le x \le 4$, x ε R}; R: {y | $-2 \le y \le 7$, y ε R}
 - **D.** D: $\{x \mid 2 < x < 4, x \in R\}$; R: $\{y \mid -2 < y < 7, y \in R\}$
- **13.** If the graph of f(x) undergoes the transformation y = f(2x + 6), the horizontal translation is:
 - A. 2 units left.
 - B. 3 units left.
 - C. 6 units left.
 - D. 12 units left.
- 14. If the point (2, 0) exists on the graph of y = f(x), what are the coordinates of the image point after the transformation y = f(-2x + 4) is applied to the graph?
 - **A.** (-3, 0)
 - **B.** (-1, 0)
 - **C.** (0, 0)
 - **D.** (1, 0)
- **15.** The graph of y = f(x) is horizontally stretched by a factor of $\frac{1}{3}$, reflected about the x-axis, and translated 2 units left. The corresponding transformation equation and mapping are:

A. Transformation Equation: y = f[-3x + 2];Mapping: $(x,y) \rightarrow \left(-\frac{1}{3}x - 2, y\right)$ B. Transformation Equation: y = -f[3x + 2];Mapping: $(x,y) \rightarrow \left(\frac{1}{3}x - 2, -y\right)$ C. Transformation Equation: y = f[-3(x + 2)];Mapping: $(x,y) \rightarrow \left(-\frac{1}{3}x - 2, y\right)$ D. Transformation Equation: y = -f[3(x + 2)];Mapping: $(x,y) \rightarrow \left(\frac{1}{3}x - 2, -y\right)$





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16. The general transformation equation y = af[b(x - h)] + k can be expressed as the mapping:

$$(x,y) \rightarrow \left(\frac{1}{b}x + h, ay + k\right)$$

Based on the mapping, one can conclude that:

A. Transformations are axis-independent.

The transformation sequence [VS - VR - VT - HS - HR - HT] is correct because all vertical transformations are grouped together and all horizontal transformations are grouped together.

B. Stretches and reflections must universally be applied before translations. The transformation sequence [VS - VR - VT - HS - HR - HT] is incorrect because a vertical translation is applied before a horizontal stretch.

C. Stretches and reflections can be applied in either order since the negative sign is included in the a and b parameters. The transformation sequence [VR - VS - VT - HR - HS - HT] is correct.

D. Both A and C are correct.

17. The goal of the video game *Space Rocks* is to pilot a spaceship through an asteroid field without colliding with any of the asteroids.

The spaceship acquires two power-ups. The first power-up halves the original width of the spaceship, making it easier to dodge asteroids. The second power-up is a left wing cannon.

What transformation describes the spaceship's new size and position *and* dodges the asteroids?

Original position of ship

Final position of ship

A. VR; VT = 7 down; HR; HS = 1/2; HT = 5 right

- **B.** HS = 1/2; HR; HT = 5 right; VR; VT = 7 down
- **C.** HT = 5 right; HR; HS = 1/2; VT = 7 down; VR
- **D.** VT = 7 down; VR; HT = 5 right; HR; HS = 1/2

Legend for Questions 16 and 17.

VS - Vertical Stretch VR - Reflection About the x-axis VT - Vertical Translation HS - Horizontal Stretch HR - Reflection About the y-axis HT - Horizontal Translation





18. The graph of f(x) is shown. The domain and range of $y = f^{-1}(x)$ is:

A. D: $\{x \mid x \ge 1, x \in R\}$; R: $\{y \mid y \ge 0, y \in R\}$ B. D: $\{x \mid x \ge 0, x \in R\}$; R: $\{y \mid y \ge 1, y \in R\}$ C. D: $\{x \mid x \le 1, x \in R\}$; R: $\{y \mid y \le 0, y \in R\}$ D. D: $\{x \mid x \le 0, x \in R\}$; R: $\{y \mid y \ge 1, y \in R\}$

19. The graph of f(x) is shown. The graph of the inverse is a function if:

A. The shape of the inverse is a parabola opening to the left.

B. A vertical line passes through the inverse graph more than once.

C. The domain of the original graph is restricted to $(-\infty, 5]$ or $[5, \infty)$, and then the graph is reflected about the line y = x.

D. The original graph is reflected about the line y = x.

20. The graph of $f(x) = -(x + 3)^2 + 1$ is shown. The inverse function is:

A.
$$x = -(y + 3)^2 + 1$$

B. $f^{-1}(x) = \sqrt{-(x-1)} - 3$ only.
C. $f^{-1}(x) = -\sqrt{-(x-1)} - 3$ only.
D. $f^{-1}(x) = \sqrt{-(x-1)} - 3$ or $f^{-1}(x) = -\sqrt{-(x-1)} - 3$, but not both together.

21. If f(x) = 2x - 6, and $f^{-1}(k) = 18$, the value of k is:

- **A.** 12
- **B.** 18
- **C.** 30
- **D.** 36

22. The formula to convert degrees Celsius to degrees Fahrenheit is $F(C) = \frac{9}{5}C + 32$. The graphs of F(C) and $F^{-1}(C)$ intersect at the point:

- **A.** (-40, -40)
- **B.** (-40, 32)
- **C.** (32, -40)
- **D.** (0, 32)









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- 23. The domain of h(x) = (f g)(x) is:
 - A. [-5, 3]B. $\{x \mid -9 \le x \le 3, x \in R\};$ C. [-5, 6]D. $\{x \mid -9 \le x \le 6, x \in R\};$
- **24.** Given the functions f(x) = x 3 and g(x) = -x + 1, the value of $\left(\frac{f}{g}\right)(5)$ is:
 - A. -2 B. $-\frac{1}{2}$ C. $\frac{1}{2}$
 - **D.** 2
- **25.** The domain and range of $h(x) = (f \cdot g)(x)$ is:
 - A. D: (0, 10]; R: [-10, 0]
 B. D: [0, 10]; R: (-10, 0]
 - **C.** D: (0, 10]; R: (-10, 0]
 - **D.** D: (-3, 10]; R: (-10, 0]
- **26.** Given the functions $f(x) = 2\sqrt{x+4} + 1$ and g(x) = -1, $(f \cdot g)(x)$ is equivalent to the transformation:
 - **A.** y = -f(x)
 - **B.** y = f(-x)
 - **C.** y = f(x) + 1
 - **D.** y = f(x) 1
- 27. Given the functions f(x) = x + 3 and $g(x) = x^2 + 6x + 9$, the function $h(x) = (f \div g)(x)$ and its domain are:
 - A. $h(x) = \frac{1}{x+3}; x \neq -3$ B. $h(x) = x+3; x \neq -3$ C. $h(x) = \frac{1}{x-3}; x \neq 3$ D. $h(x) = x-3; x \neq 3$







28. A particular cone has a height that is $\sqrt{3}$ times larger than the radius. The volume can be written as the single-variable function:



- **29.** Given the functions $f(x) = x^2 3$ and g(x) = 2x, the value of $(f \circ f)(2)$ is:
 - **A.** -16
 - **B.** -8
 - **C.** -4
 - **D.** -2
- **30.** Given the functions $f(x) = x^2 3$ and g(x) = 2x, the value of $(f \circ g)(x)$ is:
 - **A.** 2x² 3
 - **B.** 4x² 3
 - **C.** 2x² 6
 - **D.** 2x³ 6x
- **31.** Given the functions $f(x) = (x + 1)^2$ and g(x) = 3x, the composite function $n(x) = (g \circ f)(x)$ is equivalent to which transformation?
 - A. f(x) is horizontally stretched by a scale factor of three.
 - **B.** g(x) is horizontally stretched by a scale factor of three.
 - C. f(x) is vertically stretched by a scale factor of three.
 - **D.** g(x) is vertically stretched by a scale factor of three.



- 32. Given the functions $f(x) = \sqrt{x-3}$ and g(x) = x-5, the composite function $m(x) = (f \circ g)(x)$ and its domain are:
 - A. $m(x) = \sqrt{x-8}$; $D: \{x \mid x \ge 8, x \in R\}$ B. $m(x) = \sqrt{x-8}$; $D: \{x \mid x \ge 3, x \in R\}$ C. $m(x) = \sqrt{x-3} - 5$; $D: \{x \mid x \ge 8, x \in R\}$ D. $m(x) = \sqrt{x-3} - 5$; $D: \{x \mid x \ge 3, x \in R\}$
- 33. Given the functions f(x), g(x), m(x), and n(x), the composite function h(x) = [g o m o n](x) and its domain restrictions are:

A.
$$h(x) = \frac{1}{|x+2|}; x \neq -2, 0$$

B. $h(x) = \frac{1}{|x+2|}; x \neq -2$
C. $h(x) = \frac{1}{|x|(x+2)}; x \neq -2, 0$

D. $h(x) = x + 2; x \neq -2$

A. $h(x) = \sqrt{x+2}; D : [0, \infty)$ B. $h(x) = \sqrt{2x+4}; D : [0, \infty)$ C. $h(x) = \sqrt{2x+4}; D : (-2, \infty)$

D.
$$h(x) = \sqrt{2x+4}; D: [-2, \infty)$$



$$f(x) = \sqrt{x}$$
 $g(x) = \frac{1}{x}$ $m(x) = |x|$ $n(x) = x + 2$

$$f(x) = \sqrt{x}$$
 $g(x) = \frac{1}{x}$ $m(x) = |x|$ $n(x) = x + 2$

35. Given $h(x) = x^2 + 4x + 4$, where $h(x) = (f \circ g)(x)$, the functions f(x) and g(x) could be:

A. f(x) = x + 2; g(x) = x + 2B. f(x) = x - 2; g(x) = x - 2C. f(x) = x + 2; $g(x) = x^2$ D. $f(x) = x^2$; g(x) = x + 2

36. The functions f(x) = 3x - 2 and $g(x) = \frac{1}{3}x + \frac{2}{3}$ are inverses if:

- A. The graphs of f(x) and g(x) are symmetric about the line y = 0.
- **B.** $(f \cdot g)(x) = 0$
- **C.** $(f \circ g)(x) = 1$
- **D.** $(f \circ g)(x) = x$
- **37.** The price of 1 L of gasoline is \$1.05. On a level road, Darlene's car uses 0.08 L of fuel for every kilometre driven. If the volume of gas used as a function of distance is V(d) = 0.08d, and the money required for the trip as a function of volume is M(V) = 1.05V, a function that expresses the money required for the trip as a function of distance is:
 - **A.** M(d) = 0.084d
 - **B.** M(d) = 0.08d
 - **C.** M(d) = 1.05d
 - **D.** M(V) = 1.05V
- **38.** A drinking cup from a water fountain has the shape of an inverted cone. The cup has a height of 8 cm and a radius of 3 cm. The water in the cup also has the shape of an inverted cone, with a radius of r and a height of h.

The volume of the cone can be written with a single variable as:







Transformations and Operations Practice Exam - ANSWER KEY Video solutions are in italics.

1. C Basic Transformations, Example 2c	21. C Inverses, Example 7d
2. C Basic Transformations, Example 4c	22. A Inverses, Example 8 (e,f)
3. B Basic Transformations, Example 6a	23. A Function Operations, Example 1b
4. C Basic Transformations, Example 7b	24. B Function Operations, Example 2d
5. A Basic Transformations, Example 8c	25. A Function Operations, Example 3c
6. A Basic Transformations, Example 9b	26. A Function Operations, Example 4b
7. A Basic Transformations, Example 10b	27. A Function Operations, Example 6c
8. D Basic Transformations, Example 11b	28. A Function Operations, Example 9d
9. D Basic Transformations, Example 13 (c, d)	29. D Function Composition, Example 2c
10. D Basic Transformations, Example 14b	30. B Function Composition, Example 3a
11. D Combined Transformations, Example 5b (iv)	31. C Function Composition, Example 4b
12. A Combined Transformations, Example 7a	32. A Function Composition, Example 5a
13. B Combined Transformations, Example 7b	33. A Function Composition, Example 6a
14. D Combined Transformations, Example 8a	34. B Function Composition, Example 7b
15. D Combined Transformations, Example 9b	35. D Function Composition, Example 8d
16. D Combined Transformations, Example 10	36. D Function Composition, Example 9a
17. B Combined Transformations, Example 11d	37. A Function Composition, Example 10d
18. B Inverses, Example 2a	38. B Function Composition, Example 13
19. C Inverses, Example 3b	

20. D Inverses, Example 5b

Math 30-1 Practice Exam: Tips for Students

• Every question in the practice exam has already been covered in the Math 30-1 workbook. It is recommended that students refrain from looking at the practice exam until they have completed their studies for the unit.

• Do not guess on a practice exam. The practice exam is a self-diagnostic tool that can be used to identify knowledge gaps. Leave the answer blank and study the solution later.

• It is recommended that students use Udemy to access the video solutions for three reasons:

1) The videos can be downloaded faster on Udemy than the math30.ca website.

2) It is quicker to scan through each video on Udemy.

3) The Udemy app is mobile-friendly, but the math30.ca website requires Adobe Flash Player.